

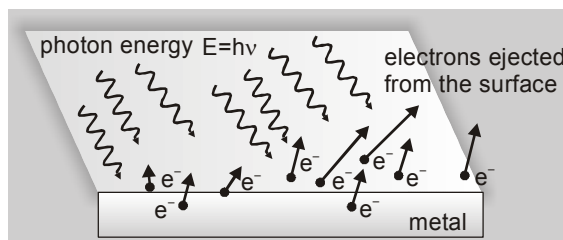
PHOTO ELECTRIC EFFECT

It is a phenomenon of ejecting electrons by falling light of suitable frequency or suitable wavelength on a metal. Ejected electron are called photoelectrons and current flowing due to the photoelectrons is called photoelectric current.

This effect was discovered by Hertz.

Laws of photo electric effect were given by Lenard.

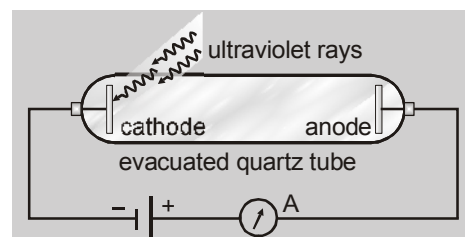
It was explained by Einstein using Quantum theory of light.



DIFFERENT EXPERIMENTS

Hertz Experiment

Hertz observed that when ultraviolet rays are incident on a negative plate of electric discharge tube then conduction takes place easily in the tube.



Hallwachs Experiment

Hallwachs observed that if negatively charged Zn plate of electroscope is illuminated by ultra violet light, its negative charge decreases and becomes neutral and after some time, it gains positive charge. It indicates that under the action of ultra violet light, some negative charged particles are emitted from the metal.

Lenard Experiment

He told that when ultraviolet rays are incident on cathode, electrons are ejected, these electrons are attracted by anode and due to complete path of photo electrons, photo current flows. When ultra violet rays are incident on anode, electrons are ejected but current does not flow.

GOLDEN KEY POINTS

- Work function :- Minimum energy required by an electron to escape from the metal surface.
- For the photo electric effect the light of short wavelength (or high frequency) is more effective than the light of long wavelength (or low frequency)
- Types of electron emission
 - (i) Thermionic emission: By suitably heating, sufficient thermal energy can be imparted to the free electrons to enable them to come out of the metal.
 - (ii) Field emission: By applying a very strong electric field (of the order of 10^8 V m^{-1}) to a metal, electrons can be pulled out of the metal, as in a spark plug.
 - (iii) Photo-electric emission: When light of suitable frequency illuminates a metal surface, electrons are emitted from the metal surface.

1. QUANTUM THEORY

1.1 Energy of Photon

Energy radiated from a source propagates (microscopically) in the form of small packets and these are known as photons. According to Planck the energy of a photon is directly proportional to the frequency of the radiation.

$$E \propto \nu$$

$$E = h\nu$$

$$E = \frac{hc}{\lambda} \quad (\because c = \nu\lambda) \quad \Rightarrow \quad E = \frac{hc}{\lambda} = \frac{12400}{\lambda} \text{ eV} - \text{\AA} \quad [\because hc = 12400 (\text{\AA} - \text{eV})]$$

Here E = energy of photon, c = speed of light, h = Planck's constant ($h = 6.62 \times 10^{-34} \text{ J-s}$),
 e = charge of electron, ν = frequency of photon, λ = wavelength of photon



1.2 Linear momentum of photon

$$\text{Linear momentum of photon } p = \frac{E}{c} = \frac{h\nu}{c} = \frac{h}{\lambda}$$

1.3 Effective mass of photon

$$\text{Effective mass of photon } m = \frac{E}{c^2} = \frac{hc}{c^2\lambda} = \frac{h}{c\lambda} \quad \text{i.e.} \quad \text{effective mass } m \propto \frac{1}{\lambda}$$

So mass of violet light photon is greater than the mass of red light photon. ($\because \lambda_R > \lambda_V$)

Rest mass of a photon is always zero.

1.4 Intensity of light

$$I = \frac{E}{At} = \frac{P}{A} \quad \dots(i)$$

$$\text{SI UNIT : } \frac{\text{joule}}{\text{m}^2 - \text{s}} \quad \text{or} \quad \frac{\text{watt}}{\text{m}^2}$$

Here P = power of source,

A = Area, t = time taken

E = energy incident in t time = $Nh\nu$,

N = number of photon incident in t time

$$\text{Intensity } I = \frac{N(h\nu)}{At} = \frac{n(h\nu)}{A} \quad \dots(ii) \quad \left[\because n = \frac{N}{t} = \text{no. of photon per sec.} \right]$$

$$\text{from equation (i) and (ii), } \frac{P}{A} = \frac{n(h\nu)}{A}$$

$$n = \frac{P}{h\nu} = \frac{P\lambda}{hc} \Rightarrow n = (5 \times 10^{24} \text{ J}^{-1} \text{ m}^{-1}) P \times \lambda$$

1.5 Radiation force and Radiation pressure

(i) When radiations are falling normally on a perfectly reflecting surface -

Let ' N ' photons are falling in time t ,

$$\text{momentum before striking the surface } (p_1) = \frac{Nh}{\lambda}$$

$$\text{momentum after striking the surface } (p_2) = -\frac{Nh}{\lambda}$$

$$\text{change in momentum of photons} = p_2 - p_1 = \frac{-2Nh}{\lambda}$$

$$\text{momentum transferred to the surface} = \Delta p = \frac{2Nh}{\lambda}$$

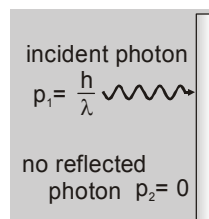
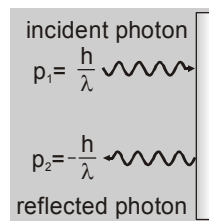
$$\text{radiation force on the surface } F = \frac{\Delta p}{\Delta t} = \frac{2Nh}{t\lambda} = n \left[\frac{2h}{\lambda} \right] \quad \text{but} \quad n = \frac{P\lambda}{hc}$$

$$\therefore F = \frac{2h}{\lambda} \times \frac{P\lambda}{hc} = \frac{2P}{c} \quad \text{and Radiation pressure} = \frac{F}{A} = \frac{2P}{cA} = \frac{2I}{c} \quad \left[\because I = \frac{P}{A} \right]$$

(ii) When radiations are falling normally on a perfectly absorbing surface -

$$\text{Radiation force } F = \frac{p_1 - p_2}{t} = \frac{\frac{Nh}{\lambda} - 0}{t} = \frac{Nh}{t\lambda} \Rightarrow F = n \frac{h}{\lambda} \quad \left[\because n = \frac{P\lambda}{hc} \right]$$

$$F = \frac{P}{c} \quad \text{and} \quad \text{Pressure} = \frac{F}{A} = \frac{P}{Ac} = \frac{I}{c}$$



Illustrations

Illustration 1.

Calculate the energy of photon having $\lambda = 4000 \text{ \AA}$ in eV and in J .

Solution.

$$E = \frac{12400}{4000} \text{ eV} = 3.1 \text{ eV}$$

$$E = 3.1 \times 1.6 \times 10^{-19} = 4.96 \times 10^{-19} \text{ J}$$

Illustration 2.

The power of a bulb is 60 milliwatt and the wavelength of light is 6000 \AA . Calculate the number of photons/second emitted by the bulb ?

Solution.

Energy released per second

$$nh\nu = \text{power} \text{ or } \frac{nhc}{\lambda} = P \text{ or } n = \frac{P\lambda}{hc} = \frac{60 \times 10^{-3} \times 6000 \times 10^{-10}}{6.62 \times 10^{-34} \times 3 \times 10^8} \text{ photon/sec} = 1.8 \times 10^{17} \text{ photon/sec}$$

Illustration 3.

The energy flux of sunlight reaching on the Earth's surface is $1.388 \times 10^3 \text{ W/m}^2$. How many photons (nearly) per square metre are incident on the Earth per second ? Assume that the photons in the sunlight have an average length of 550 nm .

Solution.

$$\text{Intensity } I = \frac{\text{Power emitted}}{\text{Area}} = \frac{P}{A} = 1.388 \times 10^3 \text{ W/m}^2$$

$$\text{Also Energy of a photon } E = \frac{hc}{\lambda} = \frac{6.63 \times 10^{-34} \times 3 \times 10^8}{550 \times 10^{-9}} = 3.616 \times 10^{-19} \text{ J}$$

$$\text{Let } n \text{ be the total number of photon/area then } n = \frac{P/A}{E} = \frac{I}{E} = \frac{1.388 \times 10^3}{3.616 \times 10^{-19}} = 3.83 \times 10^{21} \text{ photon/m}^2\text{s}$$

Illustration 4.

How many photons of wavelength $\lambda = 6600 \text{ nm}$ must strike a totally reflecting screen per second at normal incidence so as to exert a force of 1 N ?

[AIPMT Mains 2007]

Solution.

$$\text{Momentum of the incident photon } p = \frac{h}{\lambda}, \quad \text{Momentum after reflection} = -\frac{h}{\lambda}$$

$$\text{Change in momentum} = \Delta p = \frac{2h}{\lambda}$$

If n is the number of photons falling per second on the screen then force

$$F = \frac{\Delta p}{\Delta t} = \frac{2nh}{\lambda} \Rightarrow n = \frac{F\lambda}{2h} = \frac{1 \times 6600 \times 10^{-9}}{2 \times 6.6 \times 10^{-34}} = 5 \times 10^{27} \text{ photons s}^{-1}$$



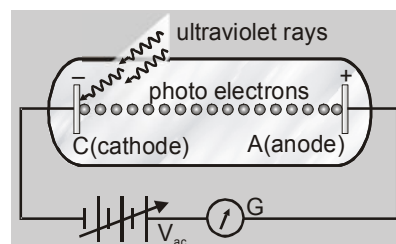
BEGINNER'S BOX-1

1. Who discovered photo electric effect ?
 (1) Hertz (2) Lenard (3) Hallwach (4) Einstein
2. The energy of a photon is equal to 3 kilo eV. Calculate its linear momentum ?
3. A parallel beam of monochromatic light of wave length 500 nm is incident normally on a perfectly absorbing surface. The power through any cross-section of the beam is 10 W. Find
 (a) Number of photon absorbed by the surface per second.
 (b) The force exerted by light beam on the surface.
4. Which colour of photon has greater energy either red or violet ?
5. A TV station is operated at 100 MW with a signal frequency of 10 MHz. Calculate the number of photons radiated per second by its antenna.
6. Calculate number of photons passing through a ring of unit area in unit time if light of intensity 100 Wm^{-2} and of wavelength 400 nm is falling normally on the ring.
7. A special kind of light bulb emits monochromatic light of wavelength 700 nm. Electrical energy supply to it at the rate of 60 W and the bulb is 50% efficient at converting that energy to light energy. How many photons are emitted by the bulb during its life time of 1 day.

2. EXPERIMENTAL STUDY OF P.E.E. BY LENARD

2.1 The effect of potential difference between A and C

Light of fixed frequency (ν) and intensity (I) is incident on photo emissive plate C, keeping A positive w.r.t. C. If positive potential of A gradually increased, it is found that first photo current increases then becomes maximum called **saturation current**.

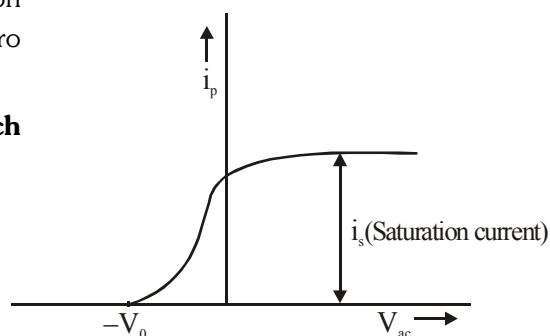


Now we apply negative potential to plate A w.r.t. C and on increasing it gradually then current decreases and becomes zero at a certain negative potential.

Magnitude of the minimum negative potential at which i_p becomes zero, called stopping potential (V_0).

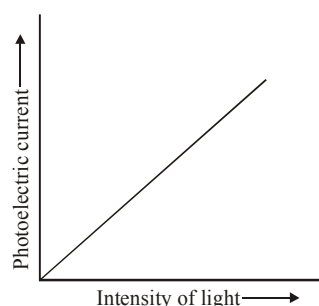
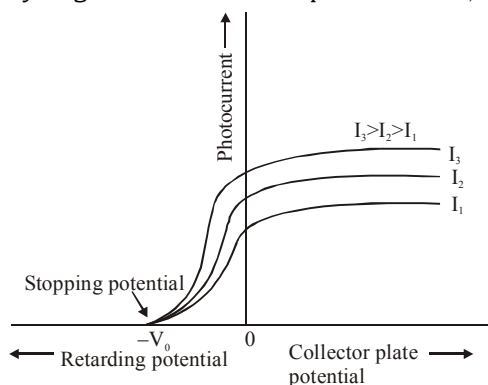
At stopping potential most energetic electrons are stopped.

It means stopping potential measures maximum kinetic energy of photo electrons. i.e. $K_{\max} = eV_0$



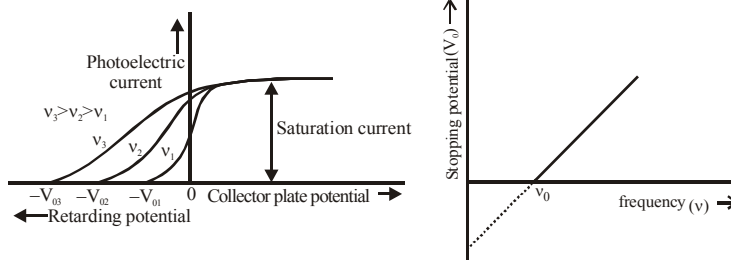
2.2 Effect of intensity of light

When intensity of given source able to produce PEE, is increased, i_s increases but V_0 remains unchanged.



2.3 Effect of frequency

When frequency of radiations is increased, V_0 increases but i_s is almost unchanged. It is also observed that below a certain frequency photoelectrons don't come out.



The minimum frequency which can eject the photo electrons is called cut off or threshold frequency.

Similarly corresponding maximum wavelength is called threshold wavelength.

2.4 Time lag : There is no time lag between the incidence of radiations and emission of electrons. It is a spontaneous process.

GOLDEN KEY POINTS

- Intensity : Energy of light passing through per unit area per unit time is known as intensity of light.

$$\text{Intensity} \propto \text{photon per second} \propto \text{electron per second} \propto \text{current} \propto \frac{1}{d^2} \quad (\text{for a given point source})$$

$$\frac{i_2}{i_1} = \frac{d_1^2}{d_2^2} \quad \begin{array}{l} i = \text{current flows in the circuit} \\ d = \text{distance between the source of light and electron emitter.} \end{array}$$

- Stopping potential does not depend on the distance between emitter and collector.
- The photoelectric emission is an instantaneous process without any apparent time lag ($\sim 10^{-9}$ s or less), even when the incident radiation is made exceedingly dim.
- Ultra violet light causes photo electric emission from any metal surface, while visible light causes photo emission from the alkali metals.
- The work function represented the energy needed to remove the least tightly bound electrons from the surface. It depends on nature of the metal and nature of surface.

3. FAILURE OF WAVE THEORY OF LIGHT

- According to wave theory when light incident on a surface, energy is distributed continuously over the surface. So that electron must take a time interval to accumulate sufficient energy to come out. But in experiment there is no time lag.
- When intensity is increased, more energetic electrons should be emitted. So that stopping potential should be intensity dependent. But it is not observed.
- According to wave theory, if intensity is sufficient then, at each frequency, electron emission is possible. It means there should not be existence of threshold frequency.

4. EXPLANATION BY EINSTEIN

4.1 Radiations absorbed by the surface are in the form of quanta (photon). Energy of each photon depends on frequency. One photon can interact with one electron at a time. In the interaction between photon and electron incident photon transfers its whole energy to the electron.

If energy is sufficient then electron comes out without any time delay. It means photo electric effect is an instantaneous process.



4.2 If intensity of the given source is increased then number of photon increases. So that, more number of electrons are emitted and greater saturation current is obtained. It means saturation current depends upon intensity of the given source $i_s \propto I$

4.3 At a time, only one photon can interact with one electron.

Energy of photon used by the electron is

$$h\nu = \text{Kinetic energy of electron} + \text{Energy required to make electron free from the metal surface } (\phi_0) + \text{Energy lost in collision before emission } (Q)$$

If $Q = 0$, means there is no heat loss, then kinetic energy of electron is maximum.

Now $h\nu = (K.E._{\text{max}}) + \phi_0$ It is known as **Einstein's equation of P.E.E.**

$$(K.E._{\text{max}}) = h\nu - \phi_0 \quad \text{or} \quad eV_0 = h\nu - \phi_0 \quad \text{or} \quad eV_0 = h\nu - h\nu_0$$

Here ν_0 is threshold frequency for that $V_0 = 0$

It means maximum K.E. and stopping potential (V_0) depends on frequency. It is independent of intensity of the given source.

4.4 Kinetic energy cannot be negative so that, $h\nu > \phi_0$

$$h\nu > h\nu_0 \quad \left[\text{Here } \phi_0 = h\nu_0 = \frac{hc}{\lambda_0}, \phi_0 = \frac{12400}{\lambda_0} \text{ eV} - \text{\AA} \right]$$

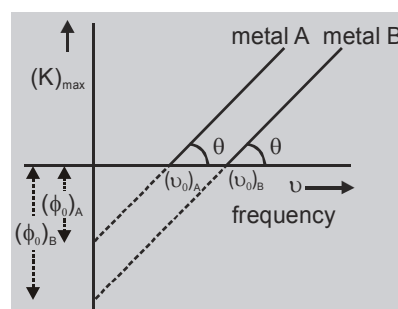
$\nu > \nu_0$ It means if frequency is less than ' ν_0 ', electron does not come out.

Graph between (K.E.)_{max} and frequency

$$(K)_{\text{max}} = h\nu - \phi_0 \quad [\because Y = mx - c]$$

slope = $m = \tan\theta = h$ (same for all metals)

$$(\phi_0)_B > (\phi_0)_A$$

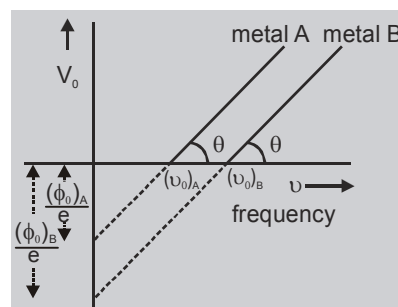


Graph between stopping potential (V_0) and frequency (ν)

$$\because eV_0 = h\nu - \phi_0$$

$$V_0 = \left[\frac{h}{e} \right] \nu - \left[\frac{\phi_0}{e} \right]$$

slope = $m = \tan\theta = \frac{h}{e}$ (same for all metals)



4.5 Quantum efficiency

$$\text{Quantum efficiency} = \frac{\text{number of electrons emitted per second}}{\text{total number of photons incident per second}} = \frac{n_e}{n_{ph}}$$

$$x = \frac{n_e}{n_{ph}} \quad \dots(i)$$

If quantum efficiency is $x\%$ then $n_e = \frac{x}{100} n_{ph}$ [from equation (i)] [Here $n_{ph} = (5 \times 10^{24} \text{ J}^{-1} \text{ m}^{-1}) P\lambda$]

4.6 Photoelectric current

$$\text{Photoelectric current } I_e = \frac{\text{charge}}{\text{time}} = \frac{Q}{t} = n_e e = 1.6 \times 10^{-19} n_e$$



GOLDEN KEY POINTS

- Einstein's Photo Electric equation is based on conservation of energy.
 - Einstein explained P.E.E. on the basis of quantum theory, for which he was awarded nobel prize.
 - According to Einstein one photon can eject one e^- only. But here the energy of incident photon should be greater than work function (threshold energy) to bring out the electron.
 - Particle nature of light is also supported by Compton effect and Raman effect.
- Compton effect :** The reduction in the energy (hence increase in wavelength) of high-energy (X-ray or gamma ray) photons when they are scattered by free electrons, or loosely bound electrons which thereby gain energy.
- Raman effect :** It is the inelastic scattering of monochromatic light as it passes through a transparent medium due to interaction of photons with the molecules of medium. This results in wavelengths being increased or decreased.

Illustrations

Illustration 5.

The threshold wavelength of a metal is 400 nm. Photo electrons have kinetic energy maximum 1.5 eV. Find the wavelength of incident photon.

Solution.

$$\lambda_0 = 400 \text{ nm} = 4000 \text{ \AA}$$

$$\text{K.E.}_{\text{max}} = \frac{12400 \text{ eV\AA}}{\lambda} - \frac{12400 \text{ eV\AA}}{\lambda_0}$$

$$1.5 \text{ eV} = \frac{12400 \text{ eV\AA}}{\lambda} - \frac{12400 \text{ eV}}{4000} \Rightarrow 1.5 \text{ eV} = \frac{12400 \text{ eV\AA}}{\lambda} - 3.1 \text{ eV}$$

$$(1.5 + 3.1) \text{ eV} = \frac{12400 \text{ eV\AA}}{\lambda} \Rightarrow \lambda = \frac{12400 \text{ \AA}}{4.6} \Rightarrow \lambda = 2696 \text{ \AA}$$

Illustration 6.

The work function of a metal is 2.3 eV and the wavelength of incident photon is $4.8 \times 10^{-7} \text{ m}$. Find maximum kinetic energy of photo electrons.

Solution.

$$\phi = 2.3 \text{ eV} \quad \text{and} \quad \lambda = 4.8 \times 10^{-7} \text{ m} = 4800 \text{ \AA}$$

$$\text{K.E.}_{\text{max}} = \frac{hc}{\lambda} - \phi = \frac{(6.62 \times 10^{-34} \text{ Js})(3 \times 10^8 \text{ ms}^{-1})}{\lambda} - \phi = \frac{12400 \text{ eV\AA}}{\lambda} - \phi$$

$$\text{K.E.}_{\text{max}} = \left[\frac{12400}{4800} - 2.3 \right] \text{ eV} \Rightarrow 0.28 \text{ eV}$$

Illustration 7.

Light quanta with an energy 4.9 eV eject photoelectrons from metal with work function 4.5 eV. Find the maximum impulse transmitted to the surface of the metal when each electron flies out.

Solution.

According to Einstein's photoelectric equation

$$K_{\text{max}} = \frac{1}{2} m v_{\text{max}}^2 = h\nu - \phi_0 = 4.9 - 4.5 = 0.4 \text{ eV}$$

$$\therefore \text{change of momentum} = \text{impulse} \therefore \text{impulse} = mv - \left(-\frac{E}{c} \right) = mv + E/c$$

$$(p_2 - p_1)$$

$$\text{Maximum impulse} = \sqrt{2mK_{\text{max}}} + \frac{E}{c}$$

$$= \sqrt{2 \times 0.4 \times 1.6 \times 10^{-19} \times 9.1 \times 10^{-31}} + \frac{4.9 \times 1.6 \times 10^{-19}}{3 \times 10^8} = 3.43 \times 10^{-25} \text{ kg m/s}$$

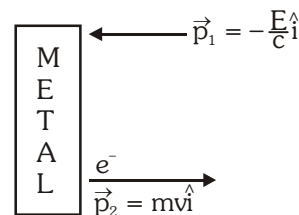


Illustration 8.

The stopping potential for the photoelectrons emitted from a metal surface of work function 1.7 eV is 10.4V. Find the wavelength of the radiation used. Also identify the energy levels in hydrogen atom which will emit this wavelength.

Solution.

$$\text{Energy of radiation } h\nu = KE_{\max} + \phi_0 = eV_0 + \phi_0 = 10.4 \text{ eV} + 1.7 \text{ eV} = 12.1 \text{ eV}$$

$$\text{Wavelength corresponding to this energy } \lambda = \frac{hc}{E} = \frac{12400}{12.1 \text{ eV}} \text{ eV-}\text{\AA} = 1024 \text{ \AA}$$

$$\text{As } \Delta E = 13.6 \left(\frac{1}{1^2} - \frac{1}{3^2} \right) = 12.1 \text{ eV}$$

so this radiation will be emitted by transition

$$n = 3 \rightarrow n = 1$$

Illustration 9.

A metallic surface is illuminated alternatively with light of wavelength 3000 Å and 6000 Å respectively. It is observed that the maximum speeds of the photoelectrons under these illuminations are in the ratio 3 : 1. Calculate the work function of the surface in eV. ($h = 6.62 \times 10^{-34}$ J-s, $c = 3 \times 10^8$ m/s)

Solution

$$\text{Maximum kinetic energy of photo electrons } K_{\max} = \frac{1}{2} mv_{\max}^2 = \frac{hc}{\lambda} - \phi_0$$

$$\text{Now let } 3000 \text{ \AA} = \lambda \text{ then } 6000 \text{ \AA} = 2\lambda$$

$$\therefore \frac{\frac{hc}{\lambda} - \phi_0}{\frac{hc}{2\lambda} - \phi_0} = \frac{(v_{\max})_1^2}{(v_{\max})_2^2} = \frac{9}{1} \Rightarrow \phi_0 = \frac{7hc}{16\lambda} = \frac{7 \times 6.62 \times 10^{-34} \times 3 \times 10^8}{16 \times 3000 \times 10^{-10} \times 1.6 \times 10^{-19}} = 1.81 \text{ eV}$$

Illustration 10.

A light of wavelength 1240 Å incident on a metal having threshold frequency 4.8×10^{14} Hz. What is maximum kinetic energy of photo electron ? If light has intensity 100 W/cm² then calculate number of incident photons per m² per second.

Solution

Maximum kinetic energy of photo electrons

$$K_{\max} = \frac{hc}{\lambda} - \phi = \frac{hc}{\lambda} - h\nu_0$$

$$K_{\max} = \frac{6.62 \times 10^{-34} \times 3 \times 10^8}{1240 \times 10^{-10} \times 1.6 \times 10^{-19}} \text{ eV} - \frac{6.62 \times 10^{-34} \times 4.8 \times 10^{14}}{1.6 \times 10^{-19}} \text{ eV}$$

$$K_{\max} = (10 - 2) \text{ eV} = 8 \text{ eV} = 12.8 \times 10^{-19} \text{ J}$$

$$\text{Number of photons per unit area per unit time } n = \frac{P\lambda}{hcA} = \frac{I\lambda}{hc}$$

$$n = \frac{100 \times 1240 \times 10^{-10}}{10^{-4} \times 6.62 \times 10^{-34} \times 3 \times 10^8} \text{ m}^{-2}\text{s}^{-1} = 62.43 \times 10^{22} \text{ m}^{-2} \text{ s}^{-1}$$



Illustration 11.

When a metal is irradiated by monochromatic light, the maximum kinetic energy of the photo-electrons is 1.2eV. If frequency of the light is increased 50% then maximum kinetic energy of photo-electron is 3.6 eV. Evaluate the workfunction of the metal.

Solution

Einstein's equation of photo electric effect is $(KE)_{\max} = h\nu - \phi_0 \Rightarrow 1.2\text{eV} = h\nu - \phi_0$

When frequency of light is increased 50% then $3.6\text{eV} = 1.5 h\nu - \phi_0$

from above equation $3.6\text{eV} = 1.5 (1.2\text{eV} + \phi_0) - \phi_0 \Rightarrow 3.6\text{eV} = 1.8\text{eV} + 0.5 \phi_0 \Rightarrow \phi_0 = 3.6\text{eV}$

Illustration 12.

A light beam of 2mW power and 6000Å wavelength incident on a photo-cell. If threshold wavelength of emitter is 7000Å and 2% incident photons eject the photo-electron then find out value of saturation current in the photo cell.

Solution

Let n photons per second incident on the emitter

$$\text{then power } P = \frac{n h c}{\lambda} \Rightarrow n = \frac{P \lambda}{h c} = \frac{2 \times 10^{-3} \times 6 \times 10^{-7}}{6.62 \times 10^{-34} \times 3 \times 10^8} = 6 \times 10^{15}$$

If per second number of emitted electrons is n_e then

$$n_e = \frac{2}{100} \times n = \frac{2}{100} \times 6 \times 10^{15} = 12 \times 10^{13}$$

$$\text{saturated current } i_s = (n_e) e = 12 \times 10^{13} \times 1.6 \times 10^{-19} = 19.2 \times 10^{-6} \text{ A}$$

Illustration 13.

The strength of magnetic field required to bend photoelectrons of maximum energy in a circle of radius 50 cm when light of wavelength 3300 Å is incident on a barium emitter is $6.7 \times 10^{-6} \text{ T}$. What value of charge on the photoelectrons is obtained from this data ?

(Given : Work function of barium = 2.5 eV; mass of the electron = $9 \times 10^{-31} \text{ kg}$) [AIPMT Mains 2007]

Solution

$$\text{Maximum KE of photoelectron } \frac{1}{2} m v_{\max}^2 = \frac{h c}{\lambda} - \phi$$

$$\begin{aligned} \Rightarrow v_{\max} &= \sqrt{\frac{2}{m} \left(\frac{h c}{\lambda} - \phi \right)} = \sqrt{\frac{2}{9 \times 10^{-31}} \left(\frac{6.6 \times 10^{-34} \times 3 \times 10^8}{3300 \times 10^{-10}} - 2.5 \times 1.6 \times 10^{-19} \right)} \\ &= \sqrt{\frac{4}{9} \times 10^{12}} = \frac{2}{3} \times 10^6 \text{ ms}^{-1} \end{aligned}$$

$$\text{Now } B e v_{\max} = \frac{M v_{\max}^2}{R_{\max}}$$

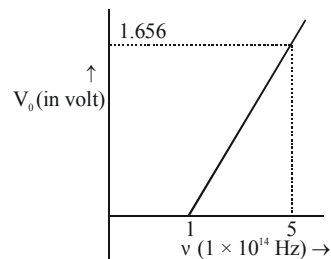
$$\Rightarrow e = \frac{M v_{\max}}{B R_{\max}} = \frac{9 \times 10^{-31} \times \frac{2}{3} \times 10^6}{6.7 \times 10^{-6} \times 0.5} = 1.8 \times 10^{-19} \text{ C}$$



Illustration 14.

The graph between the stopping potential and frequency of the incident radiation is shown in figure. Calculate. [AIPMT Mains 2008]

- (i) Planck's constant
(ii) Work function

**Solution**

- (i) According to Einstein's equation of photo electric effect $eV_0 = h\nu - h\nu_0$

$$\Rightarrow h = \frac{eV_0}{(\nu - \nu_0)} = \frac{1.6 \times 10^{-19} \times 1.656}{(5 - 1) \times 10^{14}} = \frac{1.6 \times 1.656}{4} \times 10^{-33} = 6.624 \times 10^{-34} \text{ J-s}$$

- (ii) Work function $\phi_0 = h\nu_0 = 6.624 \times 10^{-34} \times 1 \times 10^{14} = 6.624 \times 10^{-20} \text{ J}$

$$= \frac{6.624 \times 10^{-20}}{1.6 \times 10^{-19}} \text{ eV} = 0.414 \text{ eV}$$

BEGINNER'S BOX-2

- The work function of a metal is 4 eV if 5000 Å wavelength of light is incident on the metal. Is there any photo electric effect ?
- In a photo cell 4 unit photo electric current is flowing, the distance between source and cathode is 4 unit. Now distance between source and cathode becomes 1 unit. What will be photo electric current now ?
- The wavelength of photons in two cases are 4000 Å and 3600 Å respectively what is difference in stopping potential for these two ?
- Threshold frequency of a surface is ν_0 . It is illuminated by $3\nu_0$ frequency, then maximum speed of photo electrons is V m/sec. What will be maximum speed if incident frequency is $9\nu_0$?
- When incident wavelength is λ , stopping potential is $3V_0$. If incident wavelength is 2λ then stopping potential is V_0 . Find out threshold wavelength in terms of λ .
- A light beam of power 1.5 mW and 400 nm wavelength incident on a cathode. If quantum efficiency is 0.1% then, find out obtained photo current and number of photoelectron per second.
- A metallic surface of work function $h\nu$ is illuminated by a radiation beam of frequency 5ν . Stopping potential observed is X . What will be stopping potential if the surface is illuminated by radiations of 7ν frequency?
- The kinetic energy of the fastest moving photo electron from a metal of work function 2.8 eV is 2eV. If the frequency of light is doubled, then find the maximum kinetic energy of photo electron.
- A monochromatic light incident on metal 'A' having threshold frequency ν_0 . It emits photo electrons of maximum kinetic energy K . Now incident frequency is made three times and fall on a metal 'B' having threshold frequency $2\nu_0$. What will maximum kinetic energy of photo electrons emitted by metal 'B' ?
- If light of wavelength 4000 Å falls on a metal which has a stopping potential 1.4 volt against photoelectric emission then what is the work function of the metal. [Take $h = 6.6 \times 10^{-34}$ Js and $c = 3 \times 10^8$ ms⁻¹]



5. PHOTO CELL

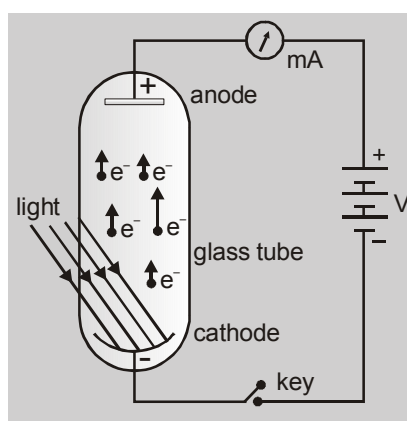
A photo cell is a practical application of the phenomenon of photo electric effect, It converts light energy into electrical energy.

Construction

A photo cell consists of an evacuated sealed glass tube containing anode and a concave cathode of suitable emitting material such as Cesium (Cs).

Working

When light of frequency greater than the threshold frequency of cathode material falls on the cathode, emitted photoelectrons are collected by the anode and an electric current starts flowing in the external circuit. The current increases with the increase in the intensity of light. The current would stop, if the light does not fall on the cathode.



Application

- (i) In television camera.
- (ii) In automatic door
- (iii) Burglar's alarm
- (iv) Automatic switching of street light and traffic signals.

MATTER WAVES THEORY

1. DUAL NATURE OF LIGHT

Experimental phenomena of light reflection, refraction, interference, diffraction are explained only on the basis of wave theory of light. These phenomena verify the wave nature of light.

Experimental phenomena of light photoelectric effect and Compton effect, pair production and pair annihilation can be explained only on the basis of the particle nature of light. These phenomena verify the particle nature of light. It is inferred that light does not have any definite nature, rather its nature depends on its experimental phenomenon. This is known as the dual nature of light. The wave nature and particle nature both can not be possible simultaneously.

2. de-Broglie HYPOTHESIS

De Broglie imagined that as light possess both wave and particle nature, similarly matter must also possess both nature, particle as well as wave.

De Broglie imagined that despite particle nature of matter, waves must also be associated with material particles. Wave associated with material particles, are defined as matter waves.

2.1 de-Broglie wavelength associated with moving particles

If a particle of mass m moving with velocity v

$$\text{Kinetic energy of the particle } E = \frac{1}{2}mv^2 = \frac{p^2}{2m}$$

$$\text{Velocity of the particle } v = \sqrt{\frac{2E}{m}}$$

$$\text{Momentum of the particle } p = mv = \sqrt{2mE}$$

$$\text{The wave length associated with the particles is } \lambda = \frac{h}{p} = \frac{h}{mv} = \frac{h}{\sqrt{2mE}}$$

The order of magnitude of wave lengths associated with macroscopic particles is 10^{-24} Å.

The smallest wavelength whose measurement is possible is that of γ - rays ($\lambda \simeq 10^{-5}$ Å). This is the reason why the wave nature of macroscopic particles is not observable.

The wavelength of matter waves associated with the microscopic particles like electron, proton, neutron, α - particle, atom, molecule etc. is of the order of 10^{-10} m, it is equal to the wavelength of X-rays, which is within the limit of measurement. Hence the wave nature of these particles is observable.

2.2 de-Broglie wavelength associated with the charged particles

Let a charged particle having charge q is accelerated by potential difference V

$$\text{Kinetic energy of this particle } E = \frac{1}{2}mv^2 = qV$$

$$\text{Momentum of particle } p = mv = \sqrt{2mE} = \sqrt{2mqV}$$

$$\text{The De Broglie wavelength associated with charged particle } \lambda = \frac{h}{p} = \frac{h}{mv} = \frac{h}{\sqrt{2mE}} = \frac{h}{\sqrt{2mqV}}$$



e.g. de-Broglie wavelength for an electron

$$m_e = 9.1 \times 10^{-31} \text{ kg}, \quad q = 1.6 \times 10^{-19} \text{ C}, \quad h = 6.62 \times 10^{-34} \text{ J-s}$$

$$\text{De Broglie wavelength associated with electron } \lambda = \frac{6.62 \times 10^{-34}}{\sqrt{2 \times 9.1 \times 10^{-31} \times 1.6 \times 10^{-19} V}} \text{ m}$$

$$\lambda = \frac{12.27 \times 10^{-10}}{\sqrt{V}} \text{ meter } \sqrt{\text{volt}} \Rightarrow \lambda = \frac{12.27}{\sqrt{V}} \text{ \AA } \sqrt{\text{volt}} \quad \text{so} \quad \lambda \propto \frac{1}{\sqrt{V}}$$

$$\text{Potential difference required to stop an electron of wavelength } \lambda \text{ is } V = \frac{150.6}{\lambda^2} \text{ volt (\AA)}^2$$

2.3 de-Broglie Wavelength Associated with Uncharged Particles

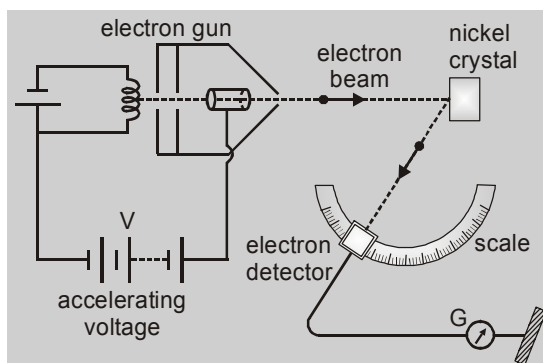
If an uncharged particle has thermal kinetic energy $E = \frac{3}{2} kT$ then its de-Broglie wavelength

$$\lambda = \frac{h}{\sqrt{2m\left(\frac{3}{2}kT\right)}} \quad \lambda = \frac{h}{\sqrt{3mkT}}$$

where k = Boltzmann's constants & T = temperature in K scale.

3. DAVISSON GERMER EXPERIMENT

The experimental arrangement is shown in figure. There are three main parts of this experiment



(i) Electron gun

Electrons of desired energy are produced in it by the process of thermionic emission.

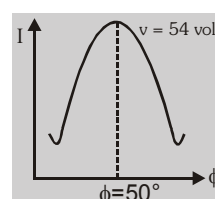
(ii) **Nickle crystal** diffracts the electrons beam obtained from electron gun. Nickle crystal behaves like a three dimensional diffraction grating

(iii) Detector (Ionisation chamber)

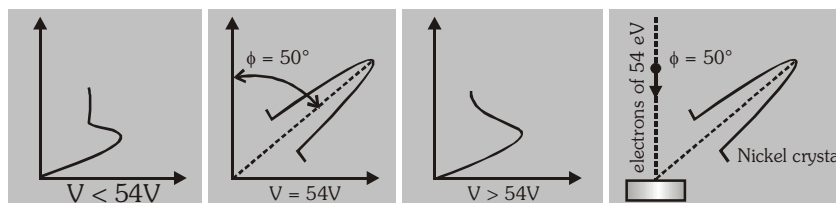
It detects the electron beam diffracted by the nickle crystal.

(iv) Conclusion and results

Curve between the intensity (I) of diffracted electrons and diffracting angle (ϕ)



Graph I versus ϕ for different accelerating potential V



In this experiment, on drawing different I- ϕ curve intensity maxima is obtained at an angle of diffraction of 50° and accelerating potential 54 volt.

From the diffraction measurements wavelength associated with electron is obtained as 1.65 \AA whereas according to de Broglie theory this wavelength comes out to be 1.66 \AA . Because both the results are same, therefore we can say wave nature is associated with the moving electrons.

diffraction from crystal is studied using two equations called Bragg's equations. This are -

$$2d \sin \theta = n\lambda \quad \text{or} \quad D \sin \phi = n\lambda$$

Where d = distance between two consecutive crystal plane

or interplanar distance.

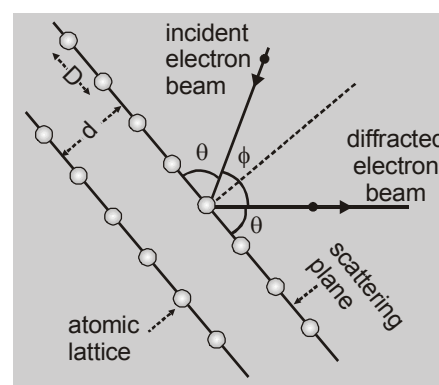
D = Distance between two atoms in the same lattice plane

n = order of diffraction

λ = De broglie wavelength associated with electron.

θ = glancing angle

ϕ = angle of diffraction



Relation between θ and ϕ : $\phi = 180^\circ - 2\theta$ or $\theta = 90^\circ - \frac{\phi}{2}$

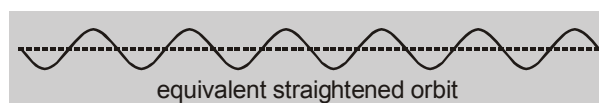
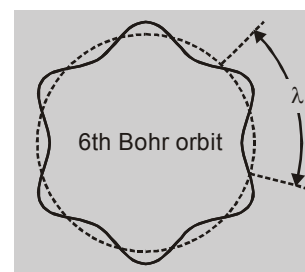
4. EXPLANATION OF BOHR QUANTISATION CONDITION

According to De Broglie electron revolves round the nucleus in the form of stationary waves (i. e. wave packet) in the similar fashion as stationary waves in a vibrating string. Electron revolves in those circular orbits whose circumference is an integral multiple of de-Broglie wavelength associated with the electron, $2\pi r = n\lambda$

$$\therefore \lambda = \frac{h}{mv} \quad \text{and} \quad 2\pi r = n\lambda$$

$$\therefore mvr = \frac{nh}{2\pi}$$

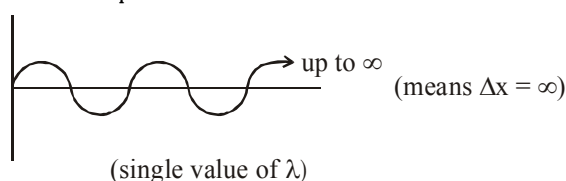
This is the Bohr quantisation condition.



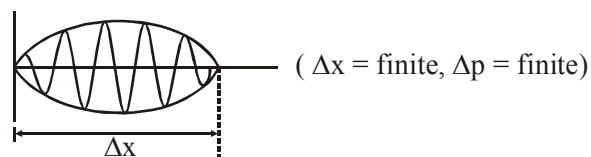
GOLDEN KEY POINTS

Quantum view of probable waves

- If a particle has definite momentum p , ($\Delta p = 0$) then it has definite wavelength $\left(\lambda = \frac{h}{p}\right)$, which extends in entire space. By max born it means particle can be find in whole universe.



But for a good description, particle should be in a finite region (means $\Delta x = \text{finite}$). So, it is rather good idea to consider a particle have group of wave (multiple value of λ) with central wavelength ' h/p '. In this case superposition of constituent wave takes place and results out as wavepacket.



Above concepts are consistent with uncertainty principle.

- Wave function of matter wave is an imaginary function ψ .
- If amplitude of matter wave is ψ then $\psi^2(\Delta V) = \text{probability of finding in } \Delta V \text{ volume}$.
- Truly satisfactory physics of dual nature of matter has not developed so far. Quantum wave theory is still subject of research.
- Observations on photoelectric effect imply that in the event of matter-light interaction, absorption of energy takes place in discrete units of $h\nu$. This is not quite the same as saying that light consists of particles, each of energy $h\nu$.
- Observations on the stopping potential (its independence of intensity and dependence on frequency) are the crucial discriminator between the wave-picture and photon-picture of photoelectric effect.
- The wavelength of a matter wave given by $\lambda = \frac{h}{p}$ has physical significance; its phase velocity v_p has no physical significance. However, the group velocity of the matter wave is physically meaningful and equals the velocity of the particle.

Illustrations

Illustration 1.

Find the initial momentum of electron if the momentum of electron is changed by P_m and the De Broglie wavelength associated with it changes by 0.50%

Solution.

$$\frac{d\lambda}{\lambda} \times 100 = 0.5 \Rightarrow \frac{d\lambda}{\lambda} = \frac{0.5}{100} = \frac{1}{200} \quad \text{and} \quad \Delta P = P_m$$

$$\because p = \frac{h}{\lambda} \quad \text{differentiating} \quad \frac{dp}{d\lambda} = -\frac{h}{\lambda^2} = -\frac{h}{\lambda} \times \frac{1}{\lambda} = -\frac{p}{\lambda} \Rightarrow \frac{|dp|}{p} = \frac{d\lambda}{\lambda}$$

$$\therefore \frac{P_m}{p} = \frac{1}{200} \Rightarrow p = 200 P_m$$

Illustration 2.

A deuteron is accelerated through a potential of 500 volts. Find the potential through which a singly ionised helium ion is to be accelerated for the same De Broglie wavelength.

Solution

$$\lambda = \frac{h}{\sqrt{2mqV}} \quad \text{or} \quad mV = \text{constant} \quad V = \text{P.d., } q \text{ is same}$$

$$m_{\text{He}} \times V_{\text{He}} = m_d V_d \quad \text{or} \quad 4V_{\text{He}} = 2 \times 500 \Rightarrow V_{\text{He}} = 250 \text{ V}$$



Illustration 3.

An α -particle moves in circular path of radius 0.83 cm. in the presence of a magnetic field of 0.25 Wb/m^2 . Find the De Broglie wavelength associated with the particle.

Solution.

$$\lambda = \frac{h}{p} = \frac{h}{qBr} = \frac{6.62 \times 10^{-34}}{2 \times 1.6 \times 10^{-19} \times 0.25 \times 83 \times 10^{-4}} \text{ meter}$$

$$\Rightarrow \lambda = 0.01 \text{ \AA} \quad \left[\because \frac{mv^2}{r} = qvB \right]$$

Illustration 4.

For what kinetic energy of a neutron will the associated de-Broglie wavelength be $1.40 \times 10^{-10} \text{ m}$? Mass of neutron is $1.675 \times 10^{-27} \text{ kg}$. ($h = 6.6 \times 10^{-34} \text{ J-s}$).

Solution.

$$\text{de-Broglie wavelength } \lambda = \frac{h}{mv} \quad \therefore v = \frac{h}{m\lambda} = \frac{6.6 \times 10^{-34}}{1.675 \times 10^{-27} \times 1.40 \times 10^{-10}} \text{ ms}^{-1}$$

$$\therefore \text{K.E. of neutron is } \frac{1}{2}mv^2 = \frac{1}{2} \times (1.675 \times 10^{-27}) \left[\frac{6.6 \times 10^{-34}}{1.675 \times 10^{-27} \times 1.40 \times 10^{-10}} \right]^2$$

$$= \frac{(6.6 \times 10^{-34})^2}{2 \times 1.675 \times 10^{-27} \times 1.4 \times 1.4 \times 10^{-20}} = 6.69 \times 10^{-21} \text{ J}$$

Illustration 5.

An electron and a photon have got the same de-Broglie wavelength. Prove that total energy of electron is greater than energy of photon.

Solution.

$$\text{Total energy of electron } E_e = mc^2 \text{ and } \lambda = \frac{h}{mv} \Rightarrow m = \frac{h}{\lambda v}$$

$$\therefore E_e = \frac{hc^2}{\lambda v}$$

$$\text{For energy of photon } E_p = \frac{hc}{\lambda} \quad \text{therefore} \quad \frac{E_e}{E_p} = \frac{hc^2}{\lambda v} \times \frac{\lambda}{hc} = \frac{c}{v} \quad \because c > v \quad \text{So } E_e > E_p$$

Illustration 6.

If λ_e and λ_p denote the de-Broglie wavelength of electron and proton after they are accelerated from rest through potential difference V_0 then find the relation between λ_e and λ_p .

Solution.

$$\therefore \text{De-Broglie wavelength } \lambda = \frac{h}{\sqrt{2mE}} = \frac{h}{\sqrt{2mqV_0}}$$

$$\text{Here } v_0 \text{ is constant so } \lambda \propto \frac{1}{\sqrt{m}} \quad \because m_p > m_e \quad \therefore \lambda_e > \lambda_p$$

OR

$$\therefore \lambda = \frac{h}{\sqrt{2mE}} = \frac{h}{\sqrt{2mqV_0}} \quad \therefore \frac{\lambda_e}{\lambda_p} = \sqrt{\frac{m_p}{m_e}}$$



Illustration**7.**

Find out ratio of wavelength for proton, deuteron and α -particle if they are accelerated through same potential difference.

Solution.

$$\begin{aligned} \therefore \lambda &= \frac{h}{\sqrt{2mE}} = \frac{h}{\sqrt{2mqV}} \quad \therefore \lambda \propto \frac{1}{\sqrt{mq}} \Rightarrow \lambda_p : \lambda_d : \lambda_\alpha = \frac{1}{\sqrt{m_p q_p}} : \frac{1}{\sqrt{m_d q_d}} : \frac{1}{\sqrt{m_\alpha q_\alpha}} \\ &= \frac{1}{\sqrt{m_p q_p}} : \frac{1}{\sqrt{2m_p q_p}} : \frac{1}{\sqrt{4m_p 2q_p}} = 1 : \frac{1}{\sqrt{2}} : \frac{1}{2\sqrt{2}} \end{aligned}$$

BEGINNER'S BOX-3

- de-Broglie wavelength of an electron, accelerated by potential V is λ . What will be de-Broglie wavelength of the electron which is accelerated by $4V$ potential?
- Find the ratio of de Broglie wavelength of molecules of hydrogen and helium which are at temperatures 27°C and 127°C respectively.
- A particle of mass M at rest decays into two particles of masses m_1 and m_2 having non zero velocities. Find out the ratio of the de-Broglie wavelengths of the two particles.
- Find out velocity of an electron so that its momentum is equal to that of photon with a wavelength of $\lambda = 5200\text{\AA}$.
- Find out voltage applied to an electron microscope to produce electron of wavelength 0.6\AA .
- What is the effective mass of a photon having wavelength λ ? [AIPMT 2006]

ANSWERS**BEGINNER'S BOX-1**

- Hertz
- $1.6 \times 10^{-24} \text{ kg-m/s}$
- (a) 2.5×10^{19} (b) $3.33 \times 10^{-8} \text{ N}$
- Violet
- 1.5×10^{34}
- 2×10^{20}
- 9×10^{24}

BEGINNER'S BOX-2

- No
- 64 unit
- 0.34 V
- 2V
- 4λ
- $0.48 \mu\text{A}$, 3×10^{12}
- 1.5 X
- 6.8 eV
- $3K + h\nu_0$
- 1.7 eV

BEGINNER'S BOX-3

- $\frac{\lambda}{2}$
- $\lambda_{\text{H}_2} : \lambda_{\text{He}} = \sqrt{8} : \sqrt{3}$
- 1 : 1
- 1400 m/s
- 416.6 volt
- $m = \frac{h}{\lambda c}$



EXERCISE-I (Conceptual Questions)

PHOTO ELECTRIC EFFECT

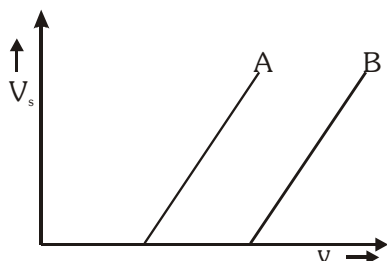
1. The energy of photon of visible light with maximum wavelength in eV is :
(1) 1 (2) 1.6
(3) 3.2 (4) 7
2. What is the momentum of a photon having frequency 1.5×10^{13} Hz :
(1) 3.3×10^{-29} kg m/s
(2) 3.3×10^{-34} kg m/s
(3) 6.6×10^{-34} kg m/s
(4) 6.6×10^{-30} kg m/s
3. The strength of photoelectric current is directly proportional to :
(1) Frequency of incident radiation
(2) Intensity of incident radiation
(3) Angle of incidence of radiation
(4) Distance between anode and cathode
4. When light is incident on surface, photo electrons are emitted. For photoelectrons :
(1) The value of kinetic energy is same for all
(2) Maximum kinetic energy do not depend on the wave length of incident light
(3) The value of kinetic energy is equal to or less than a maximum kinetic energy
(4) None of the above.
5. When light falls on a photosensitive surface, electrons are emitted from the surface. The kinetic energy of these electrons does not depend on the:
(1) Wavelength of light
(2) Frequency of light
(3) Type of material used for the surface
(4) Intensity of light
6. The work- function of a substance is 4.0 eV. The longest wavelength of light that can cause photoelectron emission from this substance is approximately :
(1) 540 nm (2) 400 nm
(3) 310 nm (4) 220 nm
7. Photoelectric effect takes place in element A. Its work function is 2.5 eV and threshold wavelength is λ . An other element B is having work function of 5 eV. Then find out the maximum wavelength that can produce photoelectric effect in B :
(1) $\lambda/2$ (2) 2λ (3) λ (4) 3λ
8. When light of wavelength lesser than 6000 Å is incident on a metal, electrons are emitted. The approximate work-function of the metal is :
(1) 1 eV (2) 2 eV (3) 4 eV (4) 6 eV
9. Surface of sodium is illuminated by a light of 6000 Å wavelength. Work function of sodium is 1.6 eV. Then minimum K.E. of emitted electrons is :
(1) 0 eV (2) 1.53 eV
(3) 2.46 eV (4) 4.14 eV
10. The maximum kinetic energy of photoelectrons emitted from a surface when photons of energy 6 eV fall on it is 4 eV. The stopping potential in volt is :
(1) 4 (2) 6 (3) 8 (4) 10
11. When a point source of monochromatic light is at a distance of 0.2 m from a photoelectric cell, the cut - off voltage and the saturation current are 0.6 volt and 18 mA respectively. If the same source is placed 0.6 m away from the photoelectric cell, then :-
(1) The stopping potential will be 0.2 V
(2) The stopping potential will be 0.6 V
(3) The saturation current will be 6 mA
(4) The saturation current will be 18 mA



12. The maximum wavelength of light for photoelectric effect from a metal is 200 nm. The maximum kinetic energy of electron which is emitted by the radiation of wave length 100 nm will be :

(1) 12.4 eV (2) 6.2 eV
(3) 100 eV (4) 200 eV

13. The stopping potential as a function of frequency of incident radiation is plotted for two different surfaces A and B. The graphs show that the work function of A is



- (1) Greater than that of B
(2) Smaller than that of B
(3) Same as that of B
(4) No comparison can be done from given graphs

14. The slope of graph drawn between stopping potential and frequency of incident light for a given surface will be :-

(1) h (2) h/e (3) eh (4) e

15. By photo electric effect, Einstein proved :-

(1) $E = h\nu$ (2) $KE = \frac{1}{2} mv^2$
(3) $E = mc^2$ (4) $E = \frac{-Rhc^2}{n^2}$

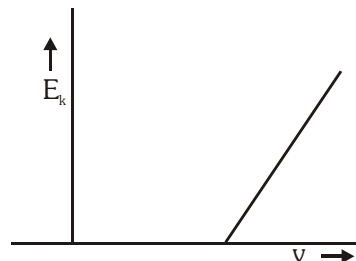
16. Which one among shows particle nature of light

(1) P.E.E. (2) Interference
(3) Refraction (4) Polarization

17. A photo-cell is illuminated by a source of light, which is placed at a distance d from the cell, If the distance become $d/2$, then number of electrons emitted per second will be :-

(1) Remain same (2) Four times
(3) Two times (4) One-fourth

18. Graph is plotted between maximum kinetic energy of electron with frequency of incident photon in Photo electric effect. The slope of curve will be :



- (1) Charge of electron
(2) Work function of metal
(3) Planck's constant
(4) Ratio of Planck constant and charge of electron

19. Photon of energy 6 eV is incident on a metal surface of work function 4 eV. Maximum KE of emitted photo electrons will be :-

(1) 0 eV (2) 1 eV (3) 2 eV (4) 10 eV

20. Light of frequency ν is incident on a metal of threshold frequency ν_0 . Then work function of metal will be :-

(1) $h\nu$ (2) $h\nu_0$
(3) $h(\nu - \nu_0)$ (4) $h(\nu + \nu_0)$

21. The work function of a photo electric material is 3.3 eV. Its threshold frequency will be :

(1) 4×10^{23} Hz (2) 8×10^{12} Hz
(3) 4×10^{11} Hz (4) 8×10^{14} Hz

22. The value of planck's constant is :-

(1) 6.63×10^{-34} J/s (2) 6.63×10^{-34} kg-m²/s
(3) 6.63×10^{-34} kg-m² (4) 6.63×10^{-34} J-s⁻¹

23. When ultraviolet rays incident on metal plate then photoelectric effect does not occur, it occurs by incidence of :-

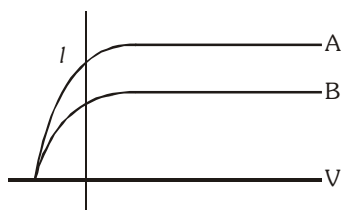
(1) Infrared rays (2) X-rays
(3) Radio wave (4) Light wave



24. A photoelectric cell is illuminated by a point source of light 1 m away. When the source is shifted to 2m then

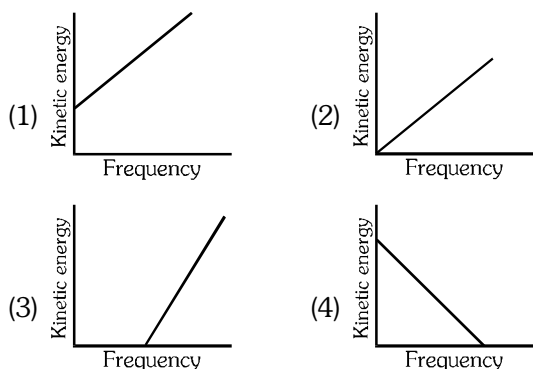
- (1) each emitted electron carries one quarter of the initial energy
- (2) number of electrons emitted is half the initial number
- (3) each emitted electron carries half the initial energy
- (4) number of electrons emitted is a quarter of the initial number

25. The graphs show the variation of current I (y-axis) in two photocell A & B as a function of the applied voltage V (x-axis) when light of same frequency is incident on the cell. Which of the following is the correct conclusion drawn from the data ?



- (1) Cathodes of the two cells are made from the same substance, the intensity of light used are different
- (2) Cathodes are made from different substances and the intensity of light is the same
- (3) Cathode substances as well as intensity of light are different
- (4) no conclusion can be drawn

26. According to Einstein's photoelectric equation, the graph between the kinetic energy of photoelectrons ejected and the frequency of incident radiation is



27. According to Einstein's photoelectric equation, the plot of the kinetic energy of the emitted photoelectrons from a metal v/s the frequency of the incident radiation gives a straight line whose slope :

- (1) depends on the intensity of the radiation
- (2) depends of the nature of the metal used
- (3) depends both on the intensity of the radiation and the metal used.
- (4) is the same for all metals and independent of the intensity of the radiation.

28. A photon of energy 4 eV is incident on a metal surface whose work function is 2eV. The minimum reverse potential to be applied for stopping the emission of electrons is

- (1) 2V
- (2) 4V
- (3) 6V
- (4) 8V

MATTER WAVES

29. If E and P are the energy and the momentum of a photon respectively then on reducing the wavelength of photon -

- (1) P and E both will decrease
- (2) P and E both will increase
- (3) P will increase and E will decrease
- (4) P will decrease and E will increase

30. If the kinetic energy of a moving particle is E , then the De Broglie wavelength is :

- (1) $h\sqrt{2mE}$
- (2) $\sqrt{\frac{2mE}{h}}$
- (3) $\frac{h}{\sqrt{2mE}}$
- (4) $\frac{hE}{\sqrt{2mE}}$

31. Electron has energy of 100 eV what will be its wavelength λ

- (1) 1.2 Å
- (2) 10 Å
- (3) 100 Å
- (4) 1 Å



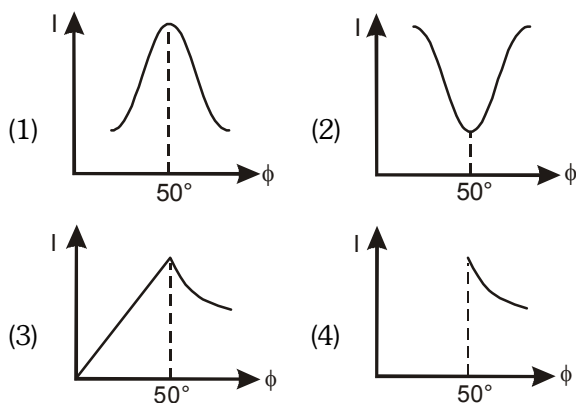
- 32.** The ratio of wavelength of deuteron and proton accelerated through the same potential difference will be -
- (1) $\frac{1}{\sqrt{2}}$ (2) $\sqrt{\frac{2}{1}}$ (3) $\frac{1}{2}$ (4) $\frac{2}{1}$
- 33.** An electron is accelerated from rest, between two points A and B at which the potentials are 20V and 40 V respectively. The De Broglie wavelength associated with the electron at B will be -
- (1) 0.75 Å (2) 7.5 Å
(3) 2.75 Å (4) 2.75 m
- 34.** An electron is moving with velocity 6.6×10^3 m/s. The De-Broglie wavelength associated with electron is (mass of electron = 9×10^{-31} Kg, Plank's Constant = 6.62×10^{-34} J-S)
- (1) 1×10^{-19} m (2) 1×10^{-5} m
(3) 1×10^{-7} m (4) 1×10^{-10} m
- 35.** The energy that should be added to an electron to reduce its De broglie wavelength from 10^{-10} m to 0.5×10^{-10} m will be :
- (1) Four times the initial energy
(2) Equal to initial energy
(3) Twice the initial energy
(4) Thrice the initial energy
- 36.** The magnitude of De broglie wavelength (λ) of electron (e), proton (p), neutron (n) and α - particle (α) all having the same kinetic energy of 1MeV, in the increasing order will follow the sequence :
- (1) $\lambda_e, \lambda_p, \lambda_n, \lambda_\alpha$ (2) $\lambda_e, \lambda_n, \lambda_p, \lambda_\alpha$
(3) $\lambda_\alpha, \lambda_n, \lambda_p, \lambda_e$ (4) $\lambda_p, \lambda_e, \lambda_\alpha, \lambda_n$
- 37.** The accelerating voltage of an electron gun is 50,000 volt. De-Broglie wavelength of the electron will be :
- (1) 0.55 Å (2) 0.055 Å
(3) 0.077 Å (4) 0.095 Å
- 38.** If the mass of neutron = 1.7×10^{-27} kg. then the De broglie wavelength of neutron of energy 3eV is :
- (1) 1.6×10^{-10} m (2) 1.6×10^{-11} m
(3) 1.4×10^{-10} m (4) 1.4×10^{-11} m
- 39.** A proton and an α - particle accelerated through same voltage. The ratio of their De-broglie wavelength will be :
- (1) 1 : 2 (2) $2\sqrt{2} : 1$ (3) $\sqrt{2} : 1$ (4) 2 : 1
- 40.** The De Broglie wavelength of an atom at absolute temperature T K will be -
- (1) $\frac{h}{mKT}$ (2) $\frac{h}{\sqrt{3mKT}}$
(3) $\frac{\sqrt{3mKT}}{h}$ (4) $\sqrt{3mKT}$
- 41.** The De-Broglie wavelength associated with electrons revolving round the nucleus in a hydrogen atom in ground state, will be-
- (1) 0.3 Å (2) 3.3 Å (3) 6.62 Å (4) 10 Å
- 42.** The wavelength of very fast moving electron ($v \approx c$) is :
- (1) $\lambda = \frac{h}{m_0 v}$ (2) $\lambda = \frac{h}{\sqrt{2mE}}$
(3) $\lambda^2 = \frac{h^2}{\sqrt{2mE}}$ (4) $\lambda = \frac{h\sqrt{1 - \frac{v^2}{c^2}}}{m_0 v}$
- 43.** Which experiment explains the wave nature of electron :-
- (1) Michelson's experiment
(2) Davisson Germer experiment
(3) Roentgen experiment
(4) Rutherford experiment



44. In Davisson-Germer experiment, the filament emits :-

- (1) Photons (2) Protons
(3) X - rays (4) Electrons

45. The correct curve between intensity of scattering (I) and the angle of diffraction ϕ in Davisson - Germer experiment is :



46. In Davisson - Germer experiment, Nickel crystal acts as :-

- (1) Perfect reflector
(2) Three dimensional diffraction grating
(3) Ideal absorber
(4) Two dimensional diffraction grating

47. The diffracted waves in the Davisson-Germer experiment are :-

- (1) Electrons (2) X - Rays
(3) Photons (4) Protons

48. An electron and a proton have the same De Broglie wavelength. Then the kinetic energy of the electron is :

- (1) zero
(2) Infinity
(3) Equal to kinetic energy of proton
(4) Greater than the kinetic energy of proton

49. De Broglie equation for an electron shows is :

- (1) Particle nature (2) Wave nature
(3) Dual nature (4) None of these

50. What will happen to De Broglie's wavelength if the velocity of electron is increased :

- (1) It will increase
(2) It will decrease
(3) It will remain same
(4) It will become twice

51. A photon of wavelength 4400 Å is passing through vacuum. The effective mass and momentum of the photon are respectively

- (1) 5×10^{-36} kg, 1.5×10^{-27} kg - m/s
(2) 5×10^{-35} kg, 1.5×10^{-26} kg - m/s
(3) zero, 1.5×10^{-26} kg - m/s
(4) 5×10^{-36} kg, 1.67×10^{-43} kg - m/s

52. Which of the following is true for photon :-

- (1) $E = \frac{hc}{\lambda}$ (2) $E = \frac{1}{2}mv^2$
(3) $P = \frac{E}{2V}$ (4) $E = \frac{1}{2}mc^2$

53. For a moving particle having kinetic energy E, the correct de Broglie wavelength is :

- (1) It is not applicable for a particle
(2) $\frac{h}{\sqrt{2mE}}$
(3) $E\sqrt{\frac{h}{2m}}$
(4) $\frac{h}{2mE}$

54. The De Broglie wavelength of an electron in the first Bohr orbit is :

- (1) Equal to the circumference of the first orbit
(2) Equal to twice the circumference of the first orbit
(3) Equal to half the circumference of the first orbit
(4) Equal to one fourth the circumference of first orbit



55. If given particles are moving with same velocity, then maximum de-Broglie wavelength for :
- (1) Proton (2) α - particle
(3) Neutron (4) β - particle
56. A proton is about 1840 times heavier than an electron. When it is accelerated by a potential difference of 1 kV, its kinetic energy will be :-
- (1) 1840 keV. (2) 1/1840 keV.
(3) 1 keV. (4) 920 keV.
57. If an electron and a photon propagate with same wavelength, it implies that can they have the same:-
- (1) Energy (2) Momentum
(3) Velocity (4) Angular momentum
58. According to De Broglie, wavelength of electron in second orbit is 10^{-9} metre. Then the circumference of orbit is :-
- (1) 10^{-9} m (2) 2×10^{-9} m
(3) 3×10^{-9} m (4) 4×10^{-9} m
59. If the mass of a microscopic particle as well as its speed are halved, the de Broglie wavelength associated with the particle will
- (1) increased by a factor more than 2
(2) increase by a factor of 2
(3) decrease by a factor of 2
(4) decrease by a factor more than 2
60. An electron and proton are accelerated through same potential, then λ_e/λ_p will be
- (1) 1 (2) m_e/m_p
(3) m_p/m_e (4) $\sqrt{m_p/m_e}$
61. An electron, proton and alpha particle have same kinetic energy. The corresponding de-Broglie wavelength would have the following relationship
- (1) $\lambda_e > \lambda_p > \lambda_\alpha$ (2) $\lambda_p > \lambda_e > \lambda_\alpha$
(3) $\lambda_\alpha > \lambda_e > \lambda_p$ (4) $\lambda_\alpha > \lambda_p > \lambda_e$
62. What is the de Broglie wavelength of an electron with a kinetic energy of 120 eV ?
- (Given : $h = 6.63 \times 10^{-34}$ J s, $m_e = 9.11 \times 10^{-31}$ kg and $e = 1.6 \times 10^{-19}$ coulomb)
- (1) 725 pm (2) 500 pm
(3) 322 pm (4) 112 pm
63. If λ_p and λ_α be the wavelengths of protons and α -particles of equal kinetic energies, then
- (1) $\lambda_p = \frac{\lambda_\alpha}{4}$ (2) $\lambda_p = \frac{\lambda_\alpha}{2}$
(3) $\lambda_p = \lambda_\alpha$ (4) $\lambda_p = 2\lambda_\alpha$

EXERCISE-I (Conceptual Questions)

Build Up Your Understanding

Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	2	1	2	3	4	3	1	2	1	1	2	2	2	2	1
Que.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans.	1	2	3	3	2	4	2	2	4	1	3	4	1	2	3
Que.	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45
Ans.	1	1	3	3	4	3	2	2	2	2	2	4	2	4	1
Que.	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
Ans.	2	1	4	3	2	1	1	2	1	4	3	2	2	1	4
Que.	61	62	63												
Ans.	1	4	4												



EXERCISE-II (Assertion & Reason)

Directions for Assertion & Reason questions

These questions consist of two statements each, printed as Assertion and Reason. While answering these Questions you are required to choose any one of the following four responses.

- (A) If both Assertion & Reason are True & the Reason is a correct explanation of the Assertion.
(B) If both Assertion & Reason are True but Reason is not a correct explanation of the Assertion.
(C) If Assertion is True but the Reason is False.
(D) If both Assertion & Reason are false.

1. **Assertion :** Photoelectric effect demonstrates the wave nature of light. [AIIMS-2004]
Reason : The number of photo electrons is proportional to the frequency of light.
(1) A (2) B (3) C (4) D
2. **Assertion :** At saturation, photoelectric current is maximum.
Reason : At saturation, All the electrons emitted from cathode are able to reach at anode.
(1) A (2) B (3) C (4) D
3. **Assertion :** In photoelectric effect, at stopping potential emission of photoelectrons is stopped.
Reason : Increase in intensity of given light increases the kinetic energy of photo -electron.
(1) A (2) B (3) C (4) D
4. **Assertion :** Work function of a metal is 8 eV. Two photons each having energy 5 eV can't eject the electron from the metal.
Reason : More than one photon can't collide simultaneously with an electron.
(1) A (2) B (3) C (4) D
5. **Assertion :** Photo electric current increases if the distance between cathode and anode is increased.
Reason : Momentum of photon is directly proportional to its wavelength.
(1) A (2) B (3) C (4) D
6. **Assertion :** A photon is not a material particle. It is a quanta of energy.
Reason : Photoelectric effect demonstrate wave nature of radiation.
(1) A (2) B (3) C (4) D
7. **Assertion :** The photoelectrons produced by a monochromatic light beam incident on a metal surface have a spread in their kinetic energies. [AIIMS 2006]
Reason : The work function of the metal varies as a function of depth from the surface.
(1) A (2) B (3) C (4) D
8. **Assertion :** The momentum of a photon is equal to $p = h/\lambda$
Reason : According to planck $E = h\nu$
According to Einstein $E = mc^2$. So that $mc^2 = h\nu \Rightarrow p = mc = h/\lambda$
(1) A (2) B (3) C (4) D
9. **Assertion :** Among the particles of same kinetic energy; lighter particle has greater de broglie wavelength.
Reason : The de-Broglie wavelength of a particle depends only on the charge of the particle.
(1) A (2) B (3) C (4) D
10. **Assertion :** A particle can behave both as a particle and wave but in a given situation, it behaves either as a particle or as a wave.
Reason : A photon and a electron have same wavelength, then the velocity of photon is less than that of the electron.
(1) A (2) B (3) C (4) D
11. **Assertion :** Speed of light is independent of frame of refrence.
Reason : Speed of light is the ultimate speed of particle.
(1) A (2) B (3) C (4) D



- 12. Assertion :-** Photoelectric effect is seen only when electron are bound. [AIIMS 2016]
Reason :- Free electron cannot absorb whole energy of photon and consuming momentum and energy.
 (1) A (2) B (3) C (4) D
- 13. Assertion :-** Electron from metal surface ejects only when light of particular wavelength will fall on surface. [AIIMS 2016]
Reason :- Light shows wave nature.
 (1) A (2) B (3) C (4) D
- 14. Assertion :-** When photons of frequency 4.3×10^{15} Hz is incident on the surface of threshold frequency 5×10^{15} Hz then no photoelectron emitted from the surface. [AIIMS 2017]
Reason :- Number of electrons ejected depends on intensity.
 (1) A (2) B (3) C (4) D
- 15. Assertion :-** On increasing the frequency of incident light on the metal surface then K.E. of ejected particle increases. [AIIMS 2017]
Reason :- Energy of photon \propto frequency of light.
 (1) A (2) B (3) C (4) D
- 16. Assertion :-** Heisenberg principle is not meaningful for moving tennis ball.
Reason :- Wave nature is not associated with moving tennis ball. [AIIMS 2018]
 (1) A (2) B (3) C (4) D
- 17. Assertion :-** Ultraviolet rays of low intensity can't emit photo electrons.
Reason :- It requires higher intensity for photo electric emission. [AIIMS 2018]
 (1) A (2) B (3) C (4) D

EXERCISE-II (Assertion & Reason)

Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	4	1	4	1	4	3	3	1	3	3	2	1	4	2	1
Que.	16	17													
Ans.	3	4													

